

# LSTM Based Power Prediction, Torque Reconstruction, and AGMA Gear Stresses Analysis for Wind Turbine Gearbox

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## Abstract

This project develops a methodology for analyzing wind turbine gearbox loading by combining Supervisory Control and Data Acquisition (SCADA) driven deep learning with standards-based gear stress calculations. A Long Short-Term Memory (LSTM) network is trained on time sequences of SCADA measurements to predict the power output of the wind turbine. The predicted power is then converted into mechanical torque at the gearbox input. Using the nominal planetary and parallel helical gear ratios and stage efficiencies, this input torque is propagated through the drivetrain to obtain torque at each intermediate shaft. From these torques, tangential tooth loads are computed and applied to the finalized gears geometry. Tangential, bending, and contact (pitting) stresses are evaluated using American Gear Manufacturers Association (AGMA) rating equations, including the relevant correction factors for overload, dynamics, size, load distribution, rim thickness, hardness ratio, temperature, and reliability. By linking SCADA based LSTM power prediction, torque reconstruction, and AGMA gear stress analysis, this work provides a physically interpretable assessment of actual tooth loadings in an operating wind turbine gearbox. On the test set, the LSTM reaches a mean absolute error of about 79.5 kW (about 3.8% of rated power), a root-mean-square error of about 126.5 kW (about 6.0% of rated power), and a coefficient of determination  $R^2 \approx 0.88$ . The reconstructed gearbox torques produce tangential tooth loads up to roughly 3.5 MN on the high-speed pinion (H1) and 0.9 MN on the intermediate pinion of the second helical stage, leading to contact stresses on the order of 1–4 GPa and bending stresses mostly below the 379 MPa (55 ksi) AGMA bending limit; these stress time series remain physically plausible and within allowable limits for all gear stages, providing an interpretable assessment of tooth loadings in an operating wind turbine gearbox.

*Keywords:* Wind power prediction, Gearbox AGMA analysis, Torque reconstruction, LSTM, Gear stress and safety factors.

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## 1. Introduction

In the field of renewable energies, wind power has emerged as a noticeable alternative, mainly due to its sustainable nature, low carbon footprint, and cost advantages [1]. However, the variable nature of wind power generation makes it difficult for the grid to maintain reliable dispatch and stable operation [2, 3, 4]. Consequently, accurately forecasting wind power decreases grid dispatching costs and enhances system performance [2, 3, 4, 5]. The complexity of forecasting wind power originates from various factors that include climate,

8 seasonal shifts, and the fluctuating patterns of wind [4]. Simultaneously, this variability  
9 transfers into fluctuating mechanical loads on the components, specifically the gearbox, which  
10 is one of the most vulnerable components to failure in the wind turbine (WT) [6, 7, 8]. Time-  
11 varying wind environment causes two major impacts on the degradation, they not only alter  
12 the rate of degradation but also introduce significant fluctuations in the amplitude of the  
13 condition monitoring signals [9].

14 As a consequence, failures in this component are a primary cause of extended downtimes  
15 and high maintenance costs, making the analysis of gear stresses necessary [7, 8, 10, 11]. In  
16 addition to this, reliability studies emphasize that gearbox gear and bearing failures account  
17 for nearly 80% of turbine drivetrain faults, underlining the importance of probabilistic reli-  
18 ability modeling that incorporates uncertain wind loads [7]. The gearbox is also one of the  
19 most expensive components; a major replacement costs roughly € 230 000, and about 26%  
20 of gearbox failures stem from gear failures [11].

21 Recent studies have extensively worked on wind turbine output prediction methods, pro-  
22 ducing a wide range of approaches, and the growth of deep learning (DL) techniques has  
23 highlighted the effectiveness of the DL models, increasingly adopting advanced machine learn-  
24 ing (ML) methods capable of capturing nonlinear patterns and time-series dependencies in  
25 wind data [2, 3]. However, modern rotating machinery operates under complex and varied  
26 conditions, making traditional methods based on mechanism analysis difficult to apply, and  
27 generally inaccurate for Remaining Useful Life (RUL) prediction [5].

28 Artificial neural networks (ANNs) are a class of predictive models widely used for pre-  
29 diction [12], recurrent neural networks (RNNs), convolutional neural networks (CNNs), and  
30 (LSTM) [4, 5, 13, 14].

31 LSTMs are foundational models of the gated recurrent network family, a class that also  
32 includes variants such as the Gated Recurrent Unit (GRU), both of which use specialized  
33 gates to manage information flow over long sequences [15].

34 Conventional forecasting methods, such as physical models (e.g., numerical weather pre-  
35 diction) and statistical models, such as autoregressive (AR), autoregressive moving average  
36 (ARMA), a model that combines AR terms with MA error terms for a stationary time-series,  
37 and autoregressive integrated moving average (ARIMA), a traditional linear statistical model  
38 for time-series forecasting, rely on explicit signal formulations and manually engineered fea-  
39 tures, which limit their ability to capture nonlinear and nonstationary behavior in wind power  
40 data. As opposed to these approaches, LSTMs introduce memory cells and gating mecha-  
41 nisms that allow them to model short-term and long-term dependencies in operational data  
42 [16, 17, 18]. In current research, many studies have relied on (SCADA) systems used for  
43 monitoring turbine components and logging operational data, and vibration data to predict  
44 time to failure [6, 19, 20, 21]. Unplanned downtime and elevated costs, resulting from poor  
45 maintenance planning, can be mitigated by accurately predicting the occurrence and timing  
46 of fatigue failure of WT components [6, 10]. Data analytics, feature extraction, and ML  
47 techniques show potential in achieving accurate prediction [6, 10, 20]. Within the techniques  
48 to predict gearbox failure, there are model-based and data-driven approaches [10, 14, 16],  
49 or a combination of the two [19]. The quality of failure prediction largely depends on the  
50 complexity and accuracy of the model, which can be further adjusted by data-driven compo-  
51 nents [6]. Recent works validated the ability of DL models to predict degradation and failure  
52 of rotating components, such as gears and bearings, using vibration datasets, while other

53 ones demonstrated SCADA DL approaches that successfully detect gearbox failures while  
54 minimizing false alarms [8, 10, 19].

55 Deep learning-based methods for failure time prediction usually require the precondition  
56 that the training and test data obey the same distribution. However, this precondition is  
57 often not met in engineering applications, as equipment operating under variable working  
58 conditions can lead to significant differences in the distribution of collected data, which  
59 degrades model performance[15].

60 Large-scale industrial studies using SCADA and vibration datasets across thousands of  
61 turbines confirmed that ANNs can predict gearbox failures up to six months in advance, sub-  
62 stantially reducing downtime and maintenance costs [6]. Approaches based on load history  
63 simulations have also been proposed as cost-effective alternatives to direct condition moni-  
64 toring, demonstrating that gearbox bearing life prediction can be estimated using simplified  
65 load-based models with minimal sensor data [20].

66 Analytical models of gearbox degradation demonstrate that failure probability grows with  
67 cumulative thermal and mechanical stresses, reinforcing the role of physics-informed moni-  
68 toring in supporting data-driven failure prediction [22].

69 Wind speed fluctuations cause uncertainty in wind power prediction and, by extension,  
70 gearbox time to failure prediction, which complicates grid operation and limits higher pene-  
71 tration of renewable energy [1, 4, 12]. Beyond system-level challenges, this variability trans-  
72 lates into fluctuating mechanical loads on turbine components, specifically the gearbox [20].  
73 Therefore, if gearbox failures can be detected or predicted in advance, operators can re-  
74 duce unplanned maintenance costs and improve turbine availability [5, 8, 23]. However, a  
75 significant challenge under these conditions is the risk of "false alarms," where signal fluctu-  
76 ations caused by high speeds can cross a fixed failure threshold prematurely, leading to an  
77 underestimation of the true predicted time to failure and unnecessary maintenance costs [9].

78 ANNs and CNNs are less appropriate for time-series forecasting and nonlinear data, such  
79 as wind power [8]. As these approaches are limited by their focus on extracting degrada-  
80 tion features from data in a single time frame, neglecting to capture valuable degradation  
81 information contained across multiple time frames, which consequently degrades estimation  
82 performance [24]. LSTM addresses this limitation through gating mechanisms that regulate  
83 information flow, allowing them to model both short-term and long-term dependencies more  
84 effectively [10, 13, 25, 26]. Studies consistently show that LSTM models outperform classical  
85 methods, such as ARIMA, in time-series forecasting, and have been successfully implemented  
86 in wind power prediction as well as machinery life estimation [10, 27].

87 By accurately predicting power output, it becomes possible to estimate the operational  
88 torque applied to the gearbox, which prior studies have used as an input to time-to-failure  
89 assessments [28]. Recent works provide evidence in this direction, demonstrating that DL  
90 can predict the service life of gears and bearings using vibration data [19], while other  
91 studies proposed DL frameworks based on SCADA data that detect gearbox failures with  
92 high accuracy and reduce false alarms [25].

93 However, most of these studies treat wind speed forecasting, power prediction, torque  
94 reconstruction, and gearbox stress analysis as separate problems. In contrast, the present  
95 work links a multivariate LSTM power-prediction model with a physics-based drivetrain and  
96 AGMA gear-rating analysis, using SCADA data to reconstruct gearbox loads and evaluate  
97 bending and contact safety factors over the operating duty cycle.

98 Various approaches have been proposed for forecasting wind power output, ranging from  
99 physical and statistical models to advanced DL techniques [5]. To overcome limitations  
100 faced by traditional models, researchers have increasingly turned to ML and DL approaches.  
101 Empirical results confirmed that LSTM consistently outperformed other architectures in fore-  
102 casting accuracy, reinforcing its suitability for sequential data [4, 18]. Beyond forecasting,  
103 it is emphasized that model-based approaches, such as fatigue crack growth and stochas-  
104 tic degradation models, are valuable for integrating physical knowledge but are limited in  
105 scalability and adaptability to operational data [29].

106 This limitation has further motivated the adoption of data-driven methods [30]. Further  
107 explored transfer learning strategies for failure time prediction, demonstrating that feature-  
108 transferred networks can adapt knowledge across machinery domains, reducing the depen-  
109 dency on large training datasets. DL frameworks have demonstrated that deep networks  
110 can extract features from vibration signals and achieve higher life prediction accuracy than  
111 shallow methods [19].

112 Even within advanced deep learning techniques, a common limitation is that many mul-  
113 tiscala models extract features from only a single time frame, failing to capture the crucial  
114 correlations of how degradation features evolve over time[24]. The polyvalence of the LSTM  
115 framework is demonstrated by its integration with attention mechanisms, which have been  
116 shown to improve feature selection under noisy environments and improve robustness in es-  
117 timation of component lifetime[16].

118 Extending beyond forecasting power output, a growing body of research has focused on  
119 gearbox reliability and failure time prediction. Reliability studies have primarily concentrated  
120 on modeling gear and bearing degradation under variable wind loads [3]. Reliability models  
121 have been used to capture stochastic stress effects [6]. Building on this, studies have proposed  
122 approaches for determining the failure time estimation of WT based on real operating data,  
123 providing practical methods for assessing gearbox reliability [20]. In industrial settings where  
124 historical failure data is often scarce, "self-data-driven" methods have emerged as a practical  
125 strategy; these approaches predict the service life of a machine based on its own operational  
126 data, without relying on examples from previously failed units [9]. More recently, SCADA-  
127 based data-driven approaches have been applied to identify degradation patterns and estimate  
128 the service life prediction [6, 27, 28]. Data-driven methods have been shown to effectively  
129 predict gearbox failures and support condition-based maintenance [6]. While supervised  
130 learning models have also shown their effectiveness with vibration measurements to assess  
131 gearbox bearing life [23]. Building on this, DL frameworks have demonstrated the ability  
132 to predict gear and bearing failure time using vibration datasets. More recently, SCADA-  
133 based approaches have been validated for accurate detection of gearbox failures, reducing  
134 false alarms [8]. A comprehensive review of life estimation approaches for rotating machinery  
135 has also emphasized the growing role of hybrid and DL frameworks in addressing variability  
136 and uncertainty [5].

137 Recent advances in prognostics and health management (PHM) have highlighted the im-  
138 portance of accurate service life prediction for rotating machinery [25]. Traditional reliability  
139 models for gearboxes often fail to take into consideration real-world variability, as noisy  
140 SCADA signals and vibration data form the basis for most life prediction efforts [11, 23].

141 ML has been applied to address gearbox failures in wind turbines, showing that accu-  
142 rate failure time prediction directly supports condition-based maintenance and reduces costly

143 downtime[6]. To better handle nonstationary and noisy vibration signals, time-frequency anal-  
 144 ysis is often used as an effective preprocessing step to reveal clearer degradation patterns.[24]  
 145 Extending this data driven approach, the combination of vibration measurements with super-  
 146 vised learning to assess gearbox bearing life further demonstrates the feasibility of data-driven  
 147 approaches for turbine drivetrains [23].

148 DL methods, particularly recurrent architectures, have shown promise in capturing tem-  
 149 poral degradation patterns. For example, studies have demonstrated that DL can extract  
 150 features from vibration signals and predict the degradation and failure of rotating compo-  
 151 nents with higher accuracy than shallow methods [19]. At the same time, review studies  
 152 emphasize the diversity of life prediction methodologies and provide a comprehensive survey  
 153 of life estimation approaches for rotating machinery, highlighting the growing role of RNNs  
 154 and other deep learning frameworks in addressing data variability and uncertainty [5]. Model-  
 155 based approaches remain valuable for integrating physical knowledge, but their limitations  
 156 in scalability and adaptability to operational data reinforce the appeal of deep architectures  
 157 [29].

158 Despite extensive work on wind turbine power prediction, SCADA-driven condition mon-  
 159 itoring, and gear failure modeling, only few studies combine data-driven power forecasting  
 160 with physics-based torque reconstruction and AGMA stress analysis. As a result, existing ap-  
 161 proaches do not provide a unified framework that links SCADA measurements, LSTM-based  
 162 prediction, and standards-based gear stress evaluation for an operating wind turbine gearbox.  
 163 This gap is particularly important because the resulting tangential loads, bending stresses,  
 164 and contact (pitting) stresses are fundamental failure-driving variables used in machinery  
 165 degradation modeling and life estimation.

166 Taken together, these findings suggest that while DL models, such as LSTMs offer a  
 167 strong framework for sequence modeling, their value appreciates when they are coupled with  
 168 physics based models of the drivetrain. Accordingly, this paper combines a multivariate  
 169 LSTM power prediction model with a physics consistent speed/torque ladder and an AGMA-  
 170 sized planetary–helical gearbox. SCADA measurements are used both to train the LSTM and  
 171 to reconstruct gearbox torque histories, from which tangential tooth loads, bending stresses,  
 172 and contact (pitting) stresses are evaluated for an operating wind turbine gearbox.

## 173 2. Methodology

### 174 2.1. Multivariate LSTM model

175 LSTM is a type of RNN designed to learn long and short-range temporal dependencies  
 176 in sequential data while avoiding the vanishing and exploding gradient problems. LSTM is  
 177 composed of memory cells that use input, forget, and output gates to regulate information  
 178 flow, enabling the network to selectively store, update, and retrieve information over long  
 179 time horizons.

180 The forget gate determines which information from the cell state shall be discarded and  
 181 is represented as

$$\mathbf{f}_t = \sigma(\mathbf{W}_f \mathbf{x}_t + \mathbf{U}_f \mathbf{h}_{t-1} + \mathbf{b}_f), \quad (1)$$

182 where  $\mathbf{x}_t \in \mathbb{R}^F$  is the input vector at time  $t$ ,  $\mathbf{h}_{t-1} \in \mathbb{R}^H$  is the previous hidden state,  $\sigma(\cdot)$   
 183 is the logistic function,  $\mathbf{W}_f \in \mathbb{R}^{H \times F}$  is the input to hidden weight matrix for the forget  
 184 gate,  $\mathbf{U}_f \in \mathbb{R}^{H \times H}$  is the recurrent weight matrix for the forget gate, and  $\mathbf{b}_f \in \mathbb{R}^H$  is the

185 corresponding bias vector. Here  $F$  denotes the number of input features and  $H$  is the number  
 186 of hidden units in the LSTM layer.

187 The input gate determines what information will be stored in the cell state, which is  
 188 represented as

$$\mathbf{i}_t = \sigma(\mathbf{W}_i \mathbf{x}_t + \mathbf{U}_i \mathbf{h}_{t-1} + \mathbf{b}_i), \quad (2)$$

189 where  $\mathbf{W}_i$ ,  $\mathbf{U}_i$ , and  $\mathbf{b}_i$  are the input-to-hidden, recurrent, and bias parameters for the input  
 190 gate, with the same dimensions as the corresponding forget-gate matrices and vectors.

191 The candidate cell update computes the candidate content to be written to the cell state,  
 192 which is represented as

$$\tilde{\mathbf{c}}_t = \tanh(\mathbf{W}_c \mathbf{x}_t + \mathbf{U}_c \mathbf{h}_{t-1} + \mathbf{b}_c), \quad (3)$$

193 where  $\tanh(\cdot)$  is the hyperbolic tangent, and  $\mathbf{W}_c$ ,  $\mathbf{U}_c$ , and  $\mathbf{b}_c$  are the input, recurrent, and  
 194 bias parameters for the candidate cell.

195 The cell state acts as a long-term memory conveyor that allows information to flow largely  
 196 intact through time, and is represented as

$$\mathbf{c}_t = \mathbf{f}_t \odot \mathbf{c}_{t-1} + \mathbf{i}_t \odot \tilde{\mathbf{c}}_t, \quad (4)$$

197 where  $\mathbf{c}_{t-1} \in \mathbb{R}^H$  is the previous cell state and  $\odot$  denotes element-wise multiplication.

198 The output gate controls what information from the cell state is passed to the output,  
 199 and is represented as

$$\mathbf{o}_t = \sigma(\mathbf{W}_o \mathbf{x}_t + \mathbf{U}_o \mathbf{h}_{t-1} + \mathbf{b}_o), \quad (5)$$

200 where  $\mathbf{W}_o$ ,  $\mathbf{U}_o$ , and  $\mathbf{b}_o$  are the input, recurrent, and bias parameters for the output gate.

201 Finally, the hidden state produces the exposed state at time  $t$ , which is represented as

$$\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{c}_t). \quad (6)$$

202 The additive update of  $\mathbf{c}_t$  creates a constant error pathway through time, enabling the  
 203 network to retain or discard information dynamically according to its relevance for future  
 204 predictions, an ability that distinguishes LSTMs from conventional RNNs. In wind turbine  
 205 SCADA datasets, the forget and input gates learn to preserve slowly varying operating con-  
 206 ditions, such as mean wind speed or rotor speed. This stable memory mechanism allows  
 207 the LSTM to capture long and short-range temporal dependencies more effectively than a  
 208 standard RNN. The three gates regulate how information flows into, through, and out of the  
 209 cell state. The forget and input gates use logistic sigmoid activations, producing values in  
 210  $(0, 1)$  that act as smooth multiplicative filters on the previous cell state and the candidate  
 211 update. The candidate update employs a tanh nonlinearity to keep the cell state bounded  
 212 and to provide expressive nonlinear representations. Finally, the output gate determines how  
 213 much of the internal cell state is revealed through the hidden state  $\mathbf{h}_t$  for subsequent layers.

214 *2.2. Gearbox design*

215 The gearbox is designed as a three-stage planetary–helical transmission that converts  
 216 the low-speed rotor torque to the high-speed generator shaft while satisfying the required  
 217 overall speed ratio. In this section, we select the stage architecture, ratio split, and key  
 218 geometric parameters, and then define the AGMA factors used for bending and contact  
 219 stress calculations. Based on the operating data, the median generator/rotor speed ratio is  
 220  $\approx 118.8$ , so the design target is set to a clean  $i_{\text{tot}} \approx 120$ . This is realized as a planetary  
 221 first stage followed by two parallel helical stages as shown in Table 1. A planetary stage  
 222 at the low–speed input is suitable for high torque because its load sharing across multiple  
 planets decreases the individual tooth loading prior to the parallel stage. The remaining

Table 1: Gearbox stage ratio breakdown

Stage	Ratio
Planetary (P)	6
Helical 1 (H1)	4
Helical 2 (H2)	5
<b>Product</b>	<b>120</b>

223 reduction ratio after the planetary stage was divided into two moderate helical stages with  
 224 ratios of 4:1 and 5:1 as shown in Table 2. This selection ensures that the pinions can employ  
 225 practical tooth counts (24 and 26 teeth) while maintaining favorable geometric properties. A  
 226 normal pressure angle of  $\phi_n = 20^\circ$  and a helix angle of  $\psi = 25^\circ$  were chosen because they are  
 227 widely used standard values. The material used is carburized and hardened steel, as shown  
 228 in Table 3, which presents the material properties.  
 229

Table 2: Key gear geometry used in the gearbox design.

Item	Symbol	Value
Normal pressure angle	$\phi_n$	$20^\circ$
Helix angle	$\psi$	$25^\circ$
Hand	–	H1: RH, H2: LH (axial thrusts opposed)
Tooth counts (H1)	$z_{p1}/z_{g1}$	$24/96 \Rightarrow i_{H1} = 4.00$
Tooth counts (H2)	$z_{p2}/z_{g2}$	$26/130 \Rightarrow i_{H2} = 5.00$

Table 3: AGMA material data used in the gearbox design for steel, carburized and hardened, Grade 1 (adapted from ANSI/AGMA 2001–D04 [31]).

Item	Symbol / Description	Value
Material	Steel, carburized and hardened	–
Grade	AGMA Grade 1 (bending & contact)	–
Modulus of elasticity	$E_p = E_g$	$30 \times 10^6$ psi
Poisson’s ratio	$\nu$	0.30
Bending strength	$S_t$ (repeated load, $10^7$ cycles)	55 000 psi
Contact strength	$S_c$ (repeated load, $10^7$ cycles)	180 000 psi
Elastic coefficient	$C_p$ (steel–steel mesh)	$2\,300 \sqrt{\text{psi}}$

230 To reduce the AGMA stresses, this gear geometry was defined for stages H1 and H2.  
 231 The nominal dimensions of this revised design are summarized in Table 4. The AGMA

Table 4: Geometry table for the Gears design.

Quantity	Symbol	H1	H2
Face width	$F$	300 mm (11.81 in)	300 mm (11.81 in)
Normal module	$m_n$	26 mm	26 mm
Transverse module	$m_t$	28.69 mm (1.13 in)	28.69 mm (1.13 in)
Helix angle	$\psi$	25°	25°
Pinion pitch diameter	$d_p$	688.5 mm (27.11 in)	745.9 mm (29.37 in)

232 method converts the nominal load into a working stress using service factors that capture  
 233 real operating and manufacturing effects, directly influencing  $S_F$ ,  $S_H$ , and the predicted  
 234 fatigue life. The overload factor  $K_o$  of 1.25 accounts for externally imposed load excursions  
 235 and duty irregularities that are not captured by the nominal transmitted tangential load  
 236  $W_t$ . In the AGMA contact–strength model, the hardness ratio factor  $C_H$  accounts for a  
 237 harder pinion running against a softer gear (ANSI/AGMA 2001–D04). When the pinion is  
 238 not harder than the gear,  $C_H = 1$ . From the specified pinion and gear Brinell hardnesses,  
 239 the present design uses the constants in Table 5: the pinions are taken with  $C_H = 1.00$  in  
 both stages, while the gears use  $C_H = 1.06$  (H1) and  $C_H = 1.07$  (H2).

Table 5: Hardness ratio factors  $C_H$  used for each mesh.

Component	Stage H1	Stage H2
Pinion	1.00	1.00
Gear	1.06	1.07

240 The reliability factor  $K_R$  modifies the allowable AGMA strength to meet a specified  
 241 reliability  $R$  (probability of survival). Higher required reliability yields a larger  $K_R$ , i.e., a  
 242 stricter allowable.  
 243

244 A design reliability of  $R = 0.99$  (99% survival) is adopted using the AGMA reliability  
 245 factor  $K_R$  values listed in Table 6.

Table 6: AGMA reliability factor  $K_R$  as a function of design reliability  $R$  (ANSI/AGMA 2001–D04; Shigley’s *Mechanical Engineering Design* [31]).

Reliability $R$	Reliability factor $K_R$
0.9999	1.50
0.999	1.25
0.99	1.00
0.90	0.85
0.50	0.70

$$K_R = 0.50 - 0.109 \ln(1 - R) \quad (0.99 \leq R \leq 0.9999), \quad (7)$$

246 The load–distribution factor  $K_m$  (face load–distribution factor) increases the working  
 247 stress to account for non-uniform load across the face width caused by mounting deflection,

248 tooth lead errors, misalignment, and housing/shaft flexibility.

$$K_m = C_{mf} = 1 + C_{mc}(C_{pf}C_{pm} + C_{ma}C_e) \quad (8)$$

249 The gearbox is classified as precision enclosed units. It is a fully enclosed, high-duty wind-  
250 turbine drivetrain with controlled mounting and alignment.

251 The resulting face load–distribution factors  $K_m$  for H1 and H2 are summarized in Table 7.

Table 7: Face load–distribution factor  $K_m$  for the precision–enclosed gearbox stages (values from AGMA 2001–D04).

Factor	Stage H1	Stage H2
$K_m$ (face load–distribution)	1.177	1.170

252

253 The size factor  $K_s$  accounts for the size effect in bending fatigue: wider/heavier sections  
254 tend to experience higher effective stress, so the working stress is multiplied by  $K_s$ .

$$K_s = \frac{1}{k_b} = 1.192 \left( \frac{F\sqrt{Y}}{P} \right)^{0.0535} \quad (9)$$

255 where  $F$  is face width (in),  $P$  is diametral pitch (1/in), and  $Y$  is the Lewis form factor.

256 The rim–thickness factor  $K_B$  is the AGMA modifier that increases bending root stress  
257 when the gear rim (backing) is thin. with  $t_r$  the minimum rim thickness beneath the root  
258 fillet and  $h_t$  the whole tooth height. following *Shigley’s Mechanical Engineering Design* [31].

$$K_B = \begin{cases} 1.6 \ln\left(\frac{2.242}{m_B}\right), & m_B < 1.2, \\ 1, & m_B \geq 1.2, \end{cases} \quad (10)$$

259 The temperature factor  $K_T$  is the AGMA temperature factor that modifies the allowable  
260 bending and contact strengths to account for elevated operating temperature. For gearboxes  
261 whose bulk oil/gear temperature does not exceed 120°C (250°F), the book specifies  $K_T = 1.0$ ;  
262 for higher temperatures,  $K_T > 1$  is used.

263 The dynamic factor  $K_v$  amplifies the working stress to account for dynamic effects in  
264 mesh (velocity error, tooth spacing/lead error, flexibility, runout).

$$K_v = \begin{cases} \left( \frac{A + \sqrt{V}}{A} \right)^B, & V \text{ in ft/min,} \\ \left( \frac{A + \sqrt{200V}}{A} \right)^B, & V \text{ in m/s,} \end{cases} \quad A = 50 + 56(1 - B), \quad B = 0.25(12 - Q_v)^{2/3}. \quad (11)$$

265 The choice of  $Q_v$  came from the accuracy/quality class of the gearing, computed  $A, B$ ,  
266 then evaluated  $K_v$ .

Table 8: Geometric quantities for helical stages H1 and H2.

Quantity	H1	H2
$Z$ (mm)	28.097248	28.561666
$m_N$	1.1049	1.0870
$I$	0.0995988424	0.1020618184

267 The geometry factors for contact (pitting) are represented by (AGMA) pitting-resistance  
 268 geometry factor  $I$ , which accounts for the local Hertzian contact geometry of a meshing pair.  
 269 For the helical stages defined in the baseline, the derived quantities are shown in Table 8.

270 The bending strength geometry factor  $J$  replaces the classical Lewis form factor in AGMA  
 271 bending fatigue; it embeds the root-fillet stress concentration and the load sharing on the  
 272 line of action.

$$J = \frac{Y}{K_f m_N}, \quad (12)$$

273 where  $K_f$  is the fillet (root) stress-concentration factor and  $m_N$  is the face-contact (load-sharing)  
 274 ratio term.

275 The resulting bending geometry factors  $J$  for the helical pinions, after applying the mod-  
 276 ifier to  $J'$ , are summarized in Table 9.

Table 9: Final bending geometry factor  $J = (\text{modifier}) \times J'$ . Values shown to 4 s.f.; H2 rounds to  $J \approx 0.570$ .

Stage	Gear ratio $i$	Mating gear teeth $N_G$	$m_G = N_G/N_P$	Modifier	$J'$	$J$
H1	4	96	4.00	0.98	0.5408	0.5300
H2	5	130	5.00	1.0053	0.5670	0.5700

277 All AGMA modifying factors used in the stress and safety-factor calculations for the  
 278 helical stages are collected in Table 10.

Table 10: Collected AGMA factors and selections used in the stress and safety calculations.

Symbol	Value	Source
$K_o$	1.25	Service class (overload).
$Q_v$	10	Quality level (precision enclosed).
$K_v$ (H1/H2)	1.092843 / 1.202365	Computed from $Q_v = 10$ with stage pitch line speeds.
$K_s$ (H1/H2)	1.150659 / 1.151928	Size factor (AGMA guidance; pinions).
$K_m$ (H1/H2)	1.176904 / 1.169501	Face load distribution (straddle mount, crowned).
$K_B$	1.00	Rim thickness factor (no thin-rim penalty).
$K_t$	1.00	Temperature factor (120 °C).
$C_f$	1.00	Surface finish factor.
$K_r$ ( $Y_z$ )	0.85	Reliability factor (90% target).
$C_p$ (U.S.)	2300.243837 $\sqrt{\text{psi}}$	Elastic coefficient (steel/steel).
$Z_E$ (SI)	191 $\sqrt{\text{MPa}}$	Elastic coefficient (SI form).
$C_H$ (pinion H1/H2)	1.00 / 1.00	Hardness ratio factor.
$C_H$ (gear H1/H2)	1.06 / 1.07	Hardness ratio factor.
$J$ (pinion H1/H2)	0.53 / 0.57	Helical $J$ via virtual tooth number $N_v$ .
$I$ (H1/H2)	0.099599 / 0.102062	With transverse $\phi_t \approx 21.88^\circ$ , $\psi = 25^\circ$ .
$Y_N, Z_N$	per duty cycles	Life factors to be applied with the duty spectrum.

279 The AGMA bending stress is defined below for both U.S. customary and SI unit systems:

$$\sigma = \begin{cases} W_t K_o K_v K_s \frac{P_t}{F} \frac{K_m K_B}{J}, & \text{U.S. customary units,} \\ W_t K_o K_v K_s \frac{1}{b m_t} \frac{K_m K_B}{J}, & \text{SI units.} \end{cases} \quad (13)$$

280 The corresponding AGMA contact stress expressions are:

$$\sigma_c = \begin{cases} C_P \sqrt{W_t K_o K_v K_s \frac{K_m C_f}{d_p F} \frac{1}{I}}, & \text{U.S. customary units,} \\ Z_E \sqrt{W_t K_o K_v K_s \frac{K_H Z_R}{d_p b} \frac{1}{Z_I}}, & \text{SI units.} \end{cases} \quad (14)$$

### 281 2.3. Data Exploration

282 The turbine's supervisory system records 10-minute sequences for electrical output and  
 283 drivetrain process, which correspond to 26064 time-ordered samples. Values in a row are  
 284 synchronous at the timestamp and represent averaged behaviour rather than instantaneous  
 285 samples, which compensates for sensor noise but also smooths fast transients. The SCADA  
 286 extract contains 26 064 ten-minute records (4344 h, 181 days), after removing rows with  
 287 missing predictor or target values, 23 821 records remain, corresponding to about 3 970 hours  
 288 ( $\approx 165$  days) of data used for wind power prediction as shown in Table 11.

Table 11: Raw SCADA data with training features for power forecasting of a wind turbine (Kelmarsch Turbine, 2021).

Date & time	Wind speed (m/s)	Energy theor. (kWh)	Rotor speed (RPM)	Wind dir. (°)	Yaw angle (°)	Power (kW)
1/1/2021 00:00	6.2047	84.5564	11.7642	304.8331	313.3654	-1.3381
1/1/2021 00:10	5.8598	71.0691	12.4192	298.8192	313.3654	-2.5933
1/1/2021 00:20	7.5828	94.7227	9.8220	305.2070	313.3654	-1.3194
1/1/2021 00:30	7.5198	96.5188	7.5376	297.4892	313.3654	-2.1187
1/1/2021 00:40	8.5198	93.4287	8.9572	287.7796	312.8034	-2.8043
1/1/2021 00:50	8.2528	89.2892	9.4874	289.5720	312.8034	-2.6143
1/1/2021 01:00	8.2058	92.5203	8.9460	289.5720	312.8034	-1.9694
... ..						
12/31/2021 23:10	6.5872	82.9531	12.4460	301.5734	312.9420	1482.3756
12/31/2021 23:20	8.5672	94.2365	12.1184	303.2874	312.9420	1334.9642
12/31/2021 23:30	8.5672	94.2365	12.1184	303.2874	312.9420	1334.9642
12/31/2021 23:40	8.5672	94.2365	12.1184	303.2874	312.9420	1334.9642

289 Power (kW) is the supervised target for the power model and an intermediate quantity  
 290 used to compute torque; it reflects both aerodynamic input and drivetrain conversion. The  
 291 gearbox speed (RPM) encodes the operating regime and is required to convert power to  
 292 torque. The transmitted torque is represented as

$$\tau_t = \frac{9549.3 P}{n}, \quad (15)$$

293 where  $P$  is the mechanical power in kilowatts and  $n$  is the shaft speed in revolutions per  
 294 minute. Drivetrain acceleration captures dynamic loading and transient events that often  
 295 precede thermal and mechanical changes. Gear oil temperature (°C) tracks sustained loading  
 296 and friction with a thermal lag, providing a slower but robust indicator of operating stress.  
 297 Gear-oil pump pressure (bar) reflects lubrication flow and back-pressure; deviations may  
 298 indicate wear, viscosity changes, or pump malfunctions. Torque (Nm) is used directly when  
 299 measured; otherwise it is reconstructed from power and RPM using (15) and serves as the  
 300 mechanical input to the AGMA gear-rating analysis, where it is converted to tangential tooth  
 301 loads and, ultimately, to pinion bending and contact stresses at each gearbox stage.

302 A concise summary of the processed SCADA dataset and the LSTM input-output con-  
 303 figuration used in this study is given in Table 12.

Table 12: Summary of the SCADA dataset and LSTM input-window configuration

Item	Value	Notes
Rows (samples)	26064	26015
Sampling period	10 min	fixed cadence
Coverage	4,500 h	≈ 187.5 days
Features used	6	listed above
LSTM window $L$	96	≈ 16 h
Overlapping windows	25920	$N - L + 1$

304 *2.4. Performance metrics*

305 Generated Power forecasting is trained with Mean Absolute Error (MAE) loss and Adam.  
 306 The evaluation metrics computed after training are the Root Mean Square Error (RMSE),  
 307 the (MAE), and the coefficient of determination  $R^2$ .

$$\text{RMSE}(\hat{y}, y) = \sqrt{\frac{1}{N} \sum_{n=1}^N |\hat{y}_n - y_n|^2}, \quad (16)$$

308 where  $N$  is the number of samples,  $y_n$  is the true (measured) target at index  $n$ ,  $\hat{y}_n$  is the  
 309 model prediction, and  $|\cdot|$  denotes absolute value.

$$\text{MAE}(\hat{y}, y) = \frac{1}{N} \sum_{n=1}^N |\hat{y}_n - y_n|, \quad (17)$$

$$R^2(\hat{y}, y) = 1 - \frac{\sum_{n=1}^N (y_n - \hat{y}_n)^2}{\sum_{n=1}^N (y_n - \bar{y})^2}, \quad (18)$$

310 where  $\bar{y} = \frac{1}{N} \sum_{n=1}^N y_n$  is the sample mean of the targets.

311 *2.5. Hyperparameters for model training and forecast horizon*

312 The LSTM model is configured for short-horizon power prediction using a small number  
 313 of manual trials on the train/validation split, selecting the configuration that produced the  
 314 lowest validation error and smooth learning curves. The tests varied the number of stacked  
 315 LSTM layers, the number of hidden units per layer, the dropout rate, and the batch size.  
 316 The lookback window length was fixed to  $L = 10$  time steps (approximately 100 minutes of  
 317 past data at a 10-minute sampling time), with a stride of 1 and a one-step-ahead forecast  
 318 horizon, i.e., the power at time  $t$  is predicted from the previous ten samples. The dataset was  
 319 divided chronologically into 70% of the samples for training, 15% for validation, and 15% for  
 320 testing, with no shuffling in order to preserve the temporal dependencies between consecutive  
 321 measurements. All input features and the target were first scaled to the interval  $[0,1]$  using  
 322 a MinMaxScaler fitted on the full dataset before the split. The network architecture consists  
 323 of three stacked LSTM layers with a progressively decreasing number of neurons, with 256  
 324 units in the first layer, 128 units in the second layer, and 64 units in the third layer, each  
 325 followed by a dropout layer with a rate of 0.3 to reduce overfitting, and a final dense layer  
 326 with a linear activation function to output continuous power values. The sequence length was  
 327 set to 10 time steps, corresponding to approximately 100 minutes of history at a 10-minute  
 328 sampling interval, and the model performs a one-step-ahead forecast of the next power value.  
 329 Model optimization was performed using the Adam optimizer with a learning rate of 0.001,  
 330 and the loss function during training was the Mean Squared Error (MSE). The batch size  
 331 was set to 16, and training was allowed to continue for a maximum of 50 epochs as shown  
 332 in Table 13, while a ModelCheckpoint callback stored the set of weights that achieved the  
 333 lowest validation loss.

Table 13: Hyperparameters used for the LSTM power prediction model in this work.

Item	Hyperparameter
Train/Val/Test split	70% / 15% / 15%
Scaling	MinMaxScaler
LSTM layers	3
Units per LSTM layer	256, 128, 64
Neurons (total)	256, 128, 64
Dropout	0.3
Sequence length $L$	10 time steps
Forecast horizon	1 step ahead (10 min)
Stride	1
Batch size	16
Optimizer	Adam
Learning rate	0.001
Loss	Mean Squared Error (MSE)
Epochs	50

334 The chosen hyperparameters represent a compromise between model capacity and robust-  
 335 ness, given the limited size of the SCADA dataset. The stacked LSTM architecture captures  
 336 nonlinear temporal dependencies in wind speed, direction, yaw angle, and rotor speed, while  
 337 a relatively short lookback window focuses the model on the most informative recent history.  
 338 Regularization (dropout and early stopping) mitigates overfitting, and the selected batch size  
 339 and optimization settings provide stable gradient updates and reasonable training time

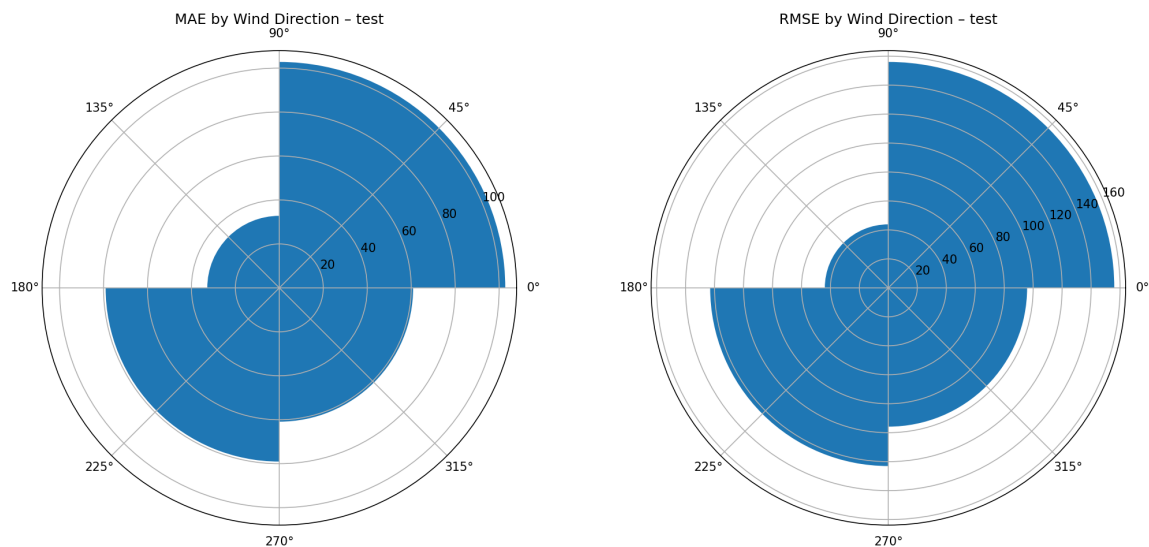
### 340 3. Results and discussion

#### 341 3.1. LSTM power prediction

342 Table 14 shows that train and validation metrics are very close, indicating that the model  
 343 experiences no obvious overfitting or data leakage. The test set coefficient of determination  
 344 is  $R^2 \approx 0.88$ , which, although lower than the train and validation values, is still strong and  
 345 promising for noisy SCADA win-power data. Additionally, the MAE and RMSE values are  
 346 of the same order of magnitude across all three splits, confirming that the model performance  
 347 is stable and consistent.

Table 14: Performance metrics of the LSTM model for power prediction.

Dataset	MAE (kW)	RMSE (kW)	$R^2$
Train Power	105.358	160.951	0.945
Validation Power	101.197	156.577	0.950
Test Power	79.461	126.544	0.878



(a) Mean Absolute Error (MAE) of test-set power predictions as a function of wind direction.

(b) Root Mean Squared Error (RMSE) of test-set power predictions as a function of wind direction.

Figure 1: Test-set power prediction errors as a function of wind direction.

348 Figures 1a and 1b summarize the model accuracy as a function of wind direction on the  
 349 test set. The MAE polar plot shows that the largest errors occur for inflow directions around  
 350 the north-east and south-west sectors, where the mean absolute error reaches values close to  
 351 100 kW, while the north-west sector exhibits the lowest MAE, below about 40 kW. A similar  
 352 pattern appears in the RMSE plot, with peak values of roughly 160 kW for the most chal-  
 353 lenging sectors and lower RMSE (around 40–80 kW) elsewhere. All directional errors remain  
 354 within approximately 5–8% of the 2.1 MW rated power, indicating that the LSTM model  
 355 maintains reasonable accuracy across the full range of wind directions. The higher errors in  
 356 specific sectors suggest that certain inflow angles are more difficult to predict, possibly due  
 357 to site-specific wake effects, local terrain, or yaw misalignment, and they highlight directions  
 358 where additional model refinement or physical correction could further improve performance.

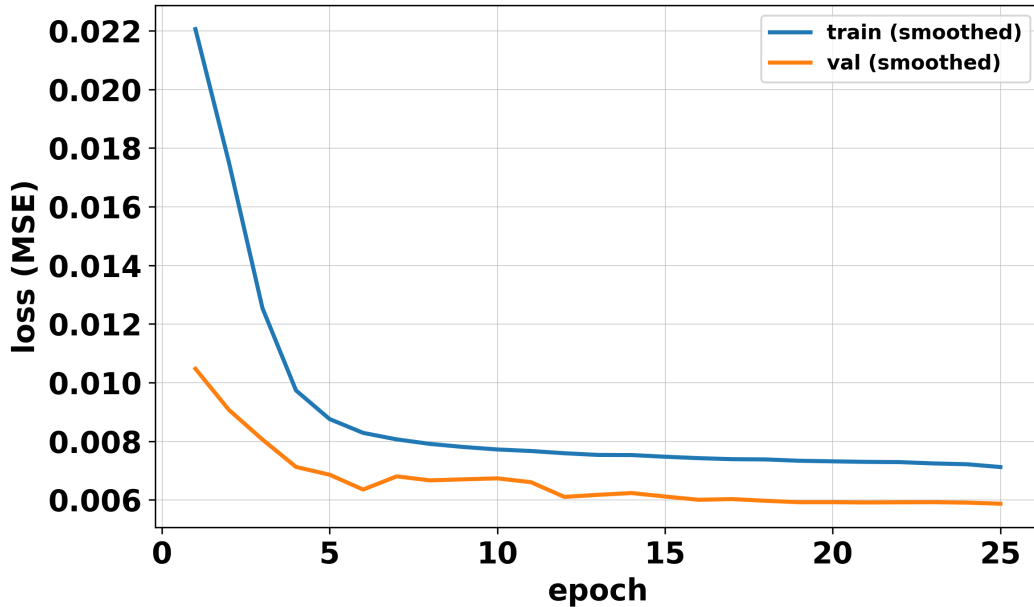


Figure 2: Training and validation loss compared epoch for the LSTM power prediction model.

359 Figure 2 shows the smoothed training and validation loss, measured as the mean squared  
 360 error (MSE) on the MinMax normalized target power (i.e., the loss values are dimensionless),  
 361 as a function of epoch for the LSTM power prediction model. Both curves exhibit a rapid  
 362 decrease during the first few epochs, with the training loss dropping from approximately  
 363  $2.2 \times 10^{-2}$  to below  $8 \times 10^{-3}$  and the validation loss decreasing from about  $1.0 \times 10^{-2}$  to  
 364 around  $6 \times 10^{-3}$ . After roughly 10–15 epochs, the losses gradually level off and no further  
 365 significant improvement is observed, indicating that the network has effectively converged.  
 366 The validation loss remains slightly lower than the training loss over almost the entire training  
 367 process, which is consistent with the use of dropout (active only during training) and with the  
 368 moving-average smoothing of the curves, and does not indicate data leakage. Importantly,  
 369 there is no late-epoch increase or divergence of the validation curve, so there is no visible  
 370 sign of overfitting. The small and stable gap between the two curves suggests that the chosen  
 371 architecture and regularisation provide a good trade-off between bias and variance for this  
 372 dataset, and that training for about 25–30 epochs is sufficient to obtain a well-trained model.

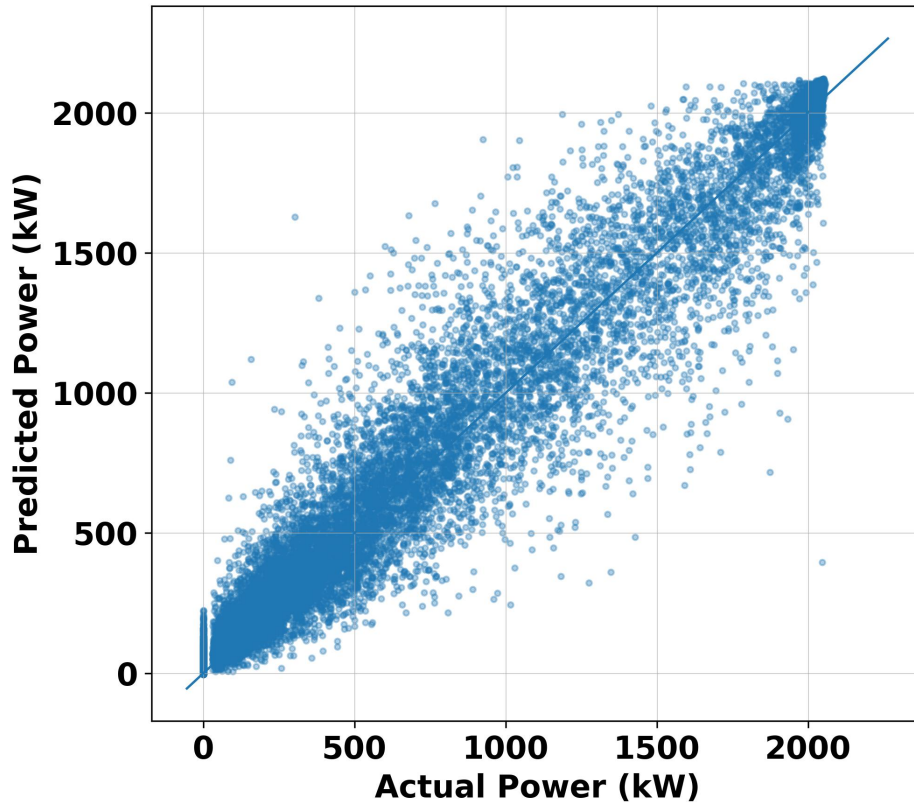


Figure 3: Predicted Power compared to Actual Power in kW(TEST)

373 Figure 3 shows that most points are concentrated around the  $45^\circ$  diagonal, indicating  
 374 that the LSTM captures the main non linear relationship between wind conditions and power  
 375 output with no obvious systematic bias.

376 The test coefficient of determination is  $R^2 \approx 0.945$ , while the mean absolute error and  
 377 root-mean-square error are approximately 79.5 kW ( $\approx 3.8\%$  of the 2.1 MW rated power) and  
 378 126.5 kW ( $\approx 6.0\%$ ), respectively. The slightly increased spread at higher power levels reflects  
 379 the reduced number of high-wind samples and the inherently higher variability of turbine  
 380 operation near rated conditions, but the overall alignment with the diagonal confirms that  
 381 the model provides a reliable short-horizon power prediction.

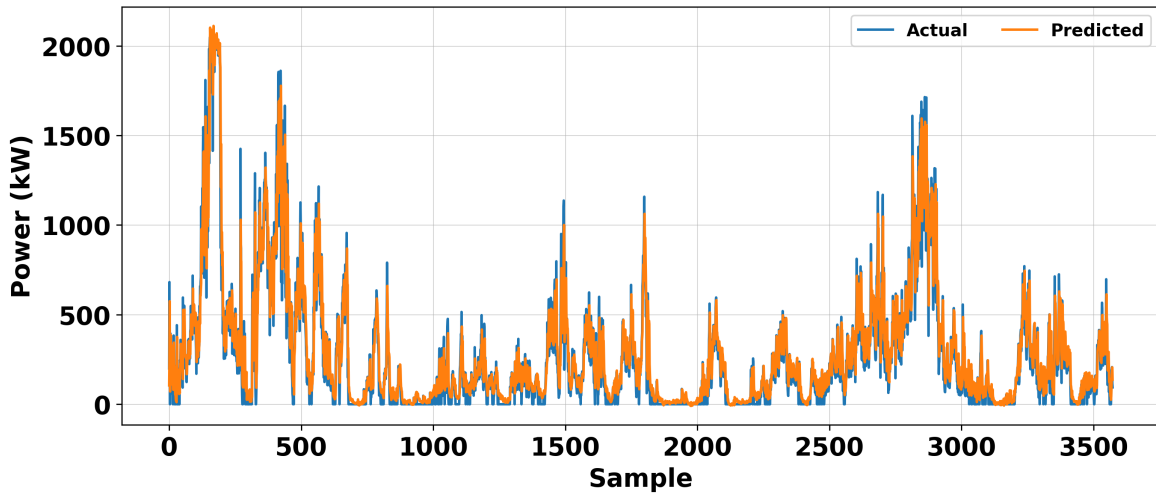


Figure 4: Actual and predicted power time series on the test set for the LSTM model.

382 Figure 4 compares the actual and predicted power time series on the test set. The two  
 383 curves almost overlap, including during high-power episodes close to the 2.1 MW rated power,  
 384 indicating that the LSTM is able to track both low-power periods and sharp ramps with  
 385 only small phase and amplitude errors. The remaining discrepancies are mainly short under  
 386 or over-predictions around fast transients, which is expected given the 10-minute SCADA  
 387 sampling and the stochastic nature of wind inflow. With a test MAE of about 79.5 kW  
 388 ( $\approx 3.8\%$  of rated) and an RMSE of roughly 126.5 kW ( $\approx 6.0\%$  of rated), the magnitude of  
 389 the errors is physically plausible and consistent with typical uncertainty levels reported for  
 390 short-horizon turbine power forecasting.

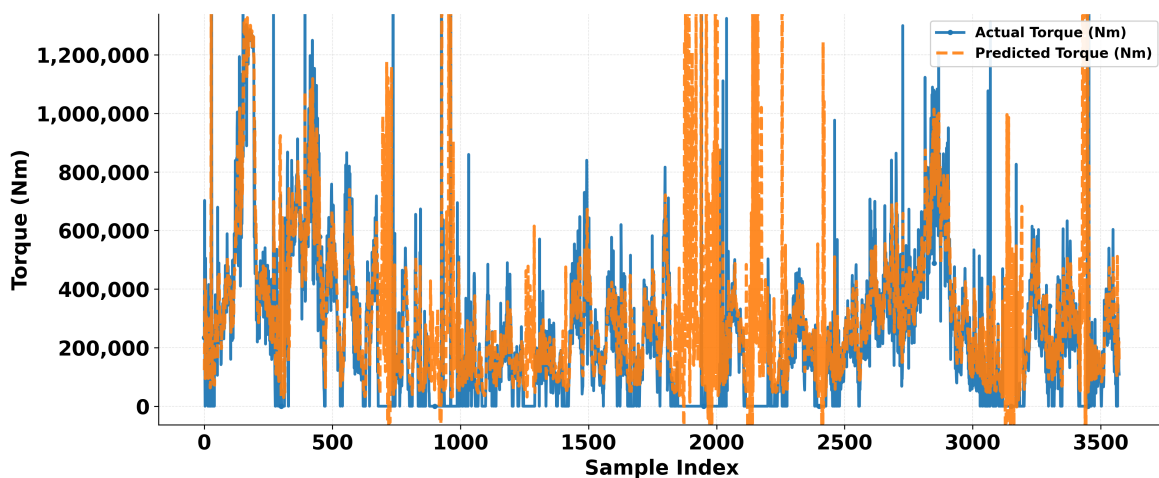


Figure 5: Actual and predicted drivetrain torque on the test set (full time series).

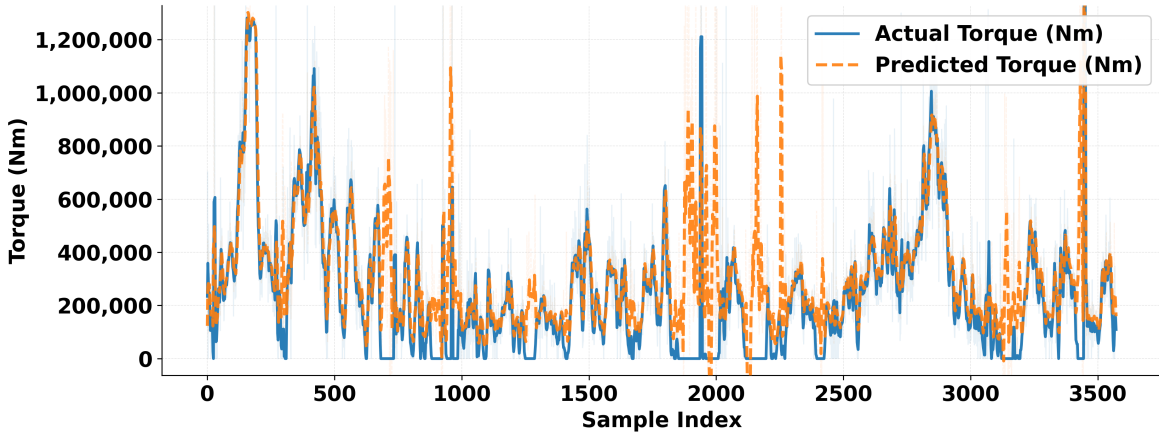


Figure 6: Smoothed and downsampled actual and predicted drivetrain torque on the test set, with percentile-based clipping for readability.

391 Figures 5 and 6 show time series of actual and predicted drivetrain torque on the test  
 392 set. After moving-average filtering, the envelopes of the two curves almost coincide, indi-  
 393 cating that the LSTM-based power prediction combined with the  $P$ -to-torque conversion  
 394 reproduces both the magnitude and temporal pattern of the torque loads. The model tracks  
 395 the main peaks and valleys of the torque history, with slight underestimation of the most  
 396 extreme spikes but good agreement in the duration and frequency of high-load events. The  
 397 torque range remains on the order of  $10^6$  Nm, which is physically plausible and realistic for a  
 398 2.1 MW turbine operating at the measured rotor speeds, confirming that the predicted torque  
 399 signals are consistent with the underlying SCADA physics rather than numerical artefacts.

### 400 3.2. Gearbox Design and AGMA Specifications

401 The reconstructed torque histories from Section 3.1 are then used as inputs to the gearbox  
 402 rating analysis. For the specified three stage planetary-helical gearbox geometry and materi-  
 403 als, the AGMA procedure is followed to compute the tangential tooth load  $W_t$ , the bending  
 404 (root) stress  $\sigma_b$ , and the contact (pitting) stress  $\sigma_c$  for each helical pinion. The stresses  
 405 are evaluated using the standard AGMA bending and surface durability forms, including all  
 406 prescribed modifying factors (overload, dynamic, size, load distribution, rim-thickness, tem-  
 407 perature, and reliability) together with the geometry factors  $J$  for bending and  $I$  for contact.  
 408 Allowable bending and contact strengths are obtained by applying the AGMA stress cycle  
 409 (life) factors  $Y_N$  and  $Z_N$  along with corrections of temperature and reliability. The time vary-  
 410 ing safety factors  $S_F(t)$  and  $S_H(t)$  are evaluated over the reconstructed duty cycle to monitor  
 411 how close the mesh operates to the allowable bending and contact strengths.

412 Figures 7 and 8 show the resulting tangential load time series  $W_t(t)$  for the Helical Stage 1  
 413 (H1) and Stage 2 (H2) pinions on the test set, plotted at the 10-minute SCADA resolution  
 414 along with a 6-point moving average. The H1 loads are consistently higher than H2, as  
 415 expected from the drivetrain ratios and efficiencies. The moving average tracks the operating  
 416 envelope, while short-duration transients appear as spikes in the raw series. The 99.5th-  
 417 percentile clipping used in subsequent plots is purely a visualization choice and is not applied  
 418 in any stress or life calculation.

419 Figures 9-12 present the corresponding bending and contact stress histories for the two  
 420 helical stages. Because both  $\sigma_b$  and  $\sigma_c$  are driven by  $W_t$ , their temporal patterns closely follow  
 421 the load curves. Bending stress is approximately proportional to  $W_t$ , whereas contact stress  
 422 varies roughly with  $\sqrt{W_t}$ , so peaks in  $\sigma_c$  are visibly compressed relative to  $\sigma_b$ . Differences  
 423 in absolute level between H1 and H2 arise from stage-specific geometry and factors such as  
 424 pitch diameter  $d$ , face width  $F$ , and the AGMA factors  $J$ ,  $I$ ,  $K_v$ , and  $K_m$ . For H1, the  
 425 6-point average of  $\sigma_b$  lies mainly near the reference level for the pinion with temporary rises  
 426 during intervals of high load, while H2 remains lower, consistent with its larger  $J$ , larger pitch  
 427 diameter, and lower stage load. Contact stress magnitudes exceed bending stress (Hertzian  
 428 pressure) but remain mostly below the chosen percentile cap.

429 The resulting bending and contact safety-factor histories for the two helical stages are  
 430 shown in Figures 13–16. These curves combine the time-varying stress demand with the  
 431 allowable strengths obtained from the upsized design. Three consistency checks are satisfied.

432 First, stage scaling is correct: H1 levels exceed H2 for  $W_t$ ,  $\sigma_b$ , and  $\sigma_c$ , matching the drivetrain  
 433 ratios and geometry.

434 Second, shape coherence holds:  $W_t(t)$ ,  $\sigma_b(t)$ , and  $\sigma_c(t)$  change together over time, with  $\sigma_c(t)$   
 435 appearing as a compressed version of the  $W_t(t)$  pattern and  $\sigma_b(t)$  nearly proportional.

436 Third, factor influence behaves as expected: with time-invariant geometry and AGMA fac-  
 437 tors, only the absolute levels differ between stages, not the temporal pattern.

438 Pinions are the limiting elements because they have fewer teeth (lower  $J$  and thus higher  
 439  $\sigma_b$  for the same  $W_t$ ), accumulate more load cycles for life factors, and in the baseline configu-  
 440 ration the mating gears benefit from hardness ratio effects. Verifying the pinions is therefore  
 441 conservative. The same computational pipeline could be applied to gears by substituting the  
 442 gear geometry ( $J$ , diameters, and life factors); the  $\sigma_c(t)$  timeline is unchanged, but it would  
 443 be compared against the gear allowables instead. For the upsized pinions considered here,  
 444 the time varying bending and contact safety factors  $S_F(t)$  and  $S_H(t)$  remain greater than  
 445 unity over all observed operating points, supporting the conclusion that the gearbox design  
 446 is sufficient for the intended service life under the reconstructed torque spectrum.

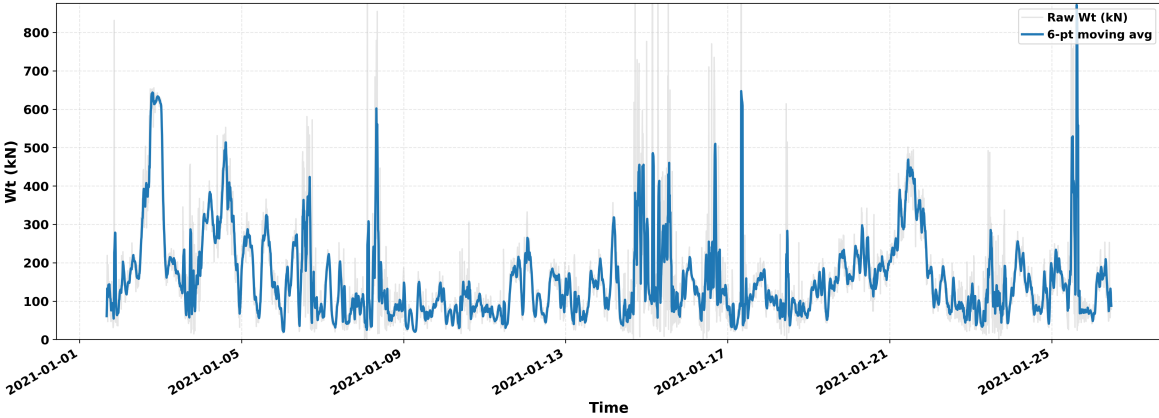


Figure 7: Tangential load  $W_t$  time series for Helical Stage 1 (H1) pinion on the test set, showing raw 10-minute values and the 6-point moving average.

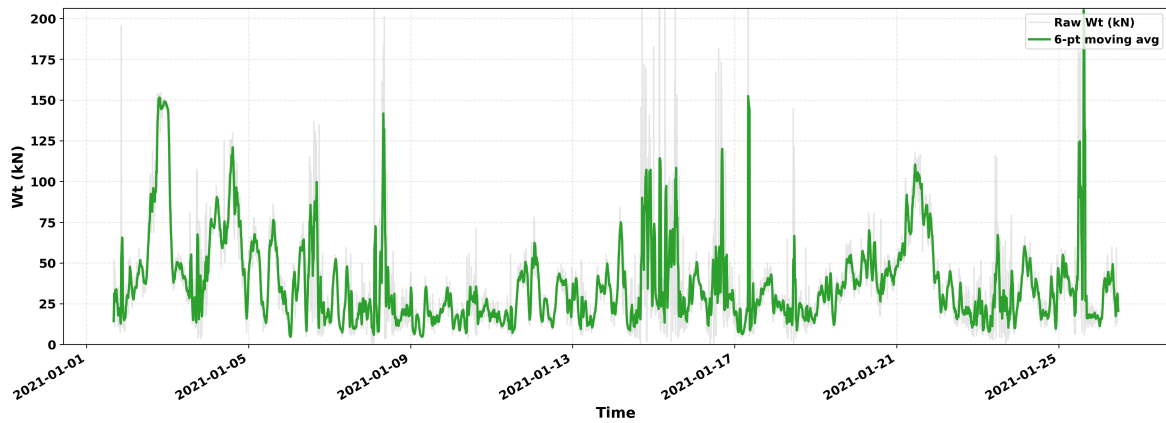


Figure 8: Tangential load  $W_t$  time series for Helical Stage 2 (H2) pinion on the test set, showing raw 10-minute values and the 6-point moving average.

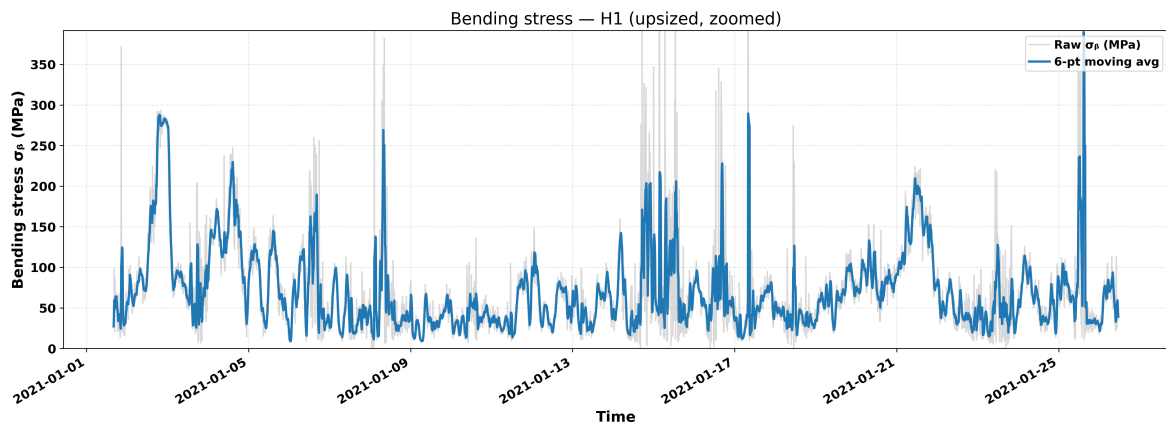


Figure 9: Bending stress time series for Helical Stage 1 (H1) pinion on the test set, showing raw values, 6-point moving average, and the 99.5th percentile cap.

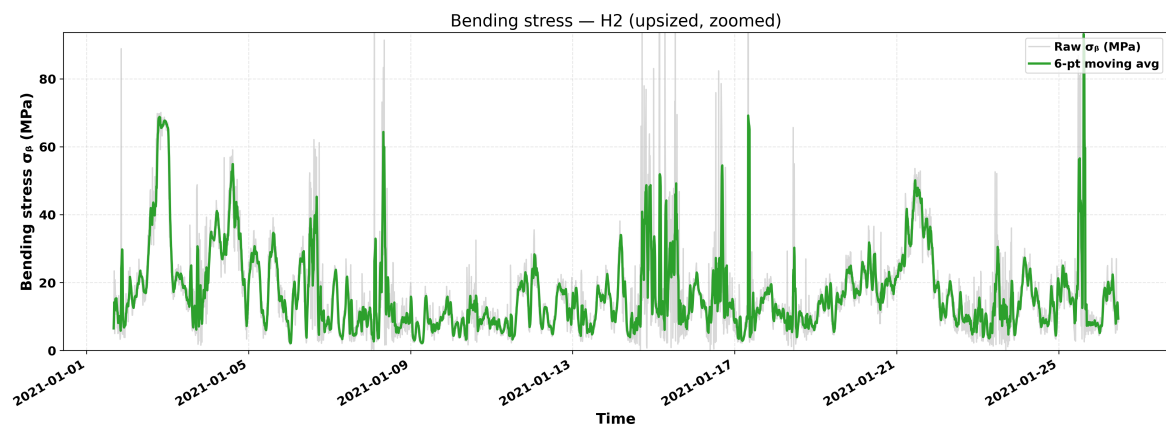


Figure 10: Bending stress time series for Helical Stage 2 (H2) pinion on the test set, showing raw values, 6-point moving average, and the 99.5th percentile cap.

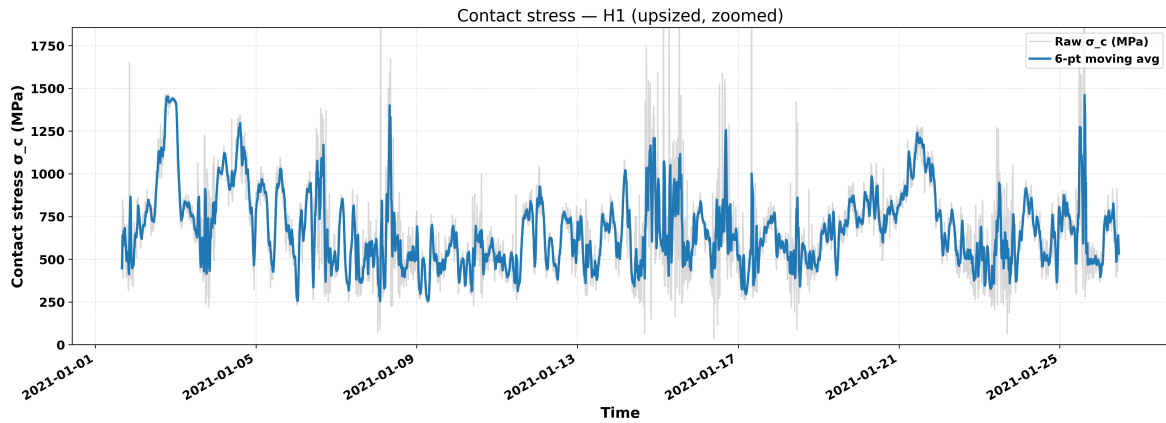


Figure 11: Contact stress  $\sigma_c$  time series for Helical Stage 1 (H1) pinion on the test set, showing raw values capped at the 99.5th percentile and the 6-point moving average.

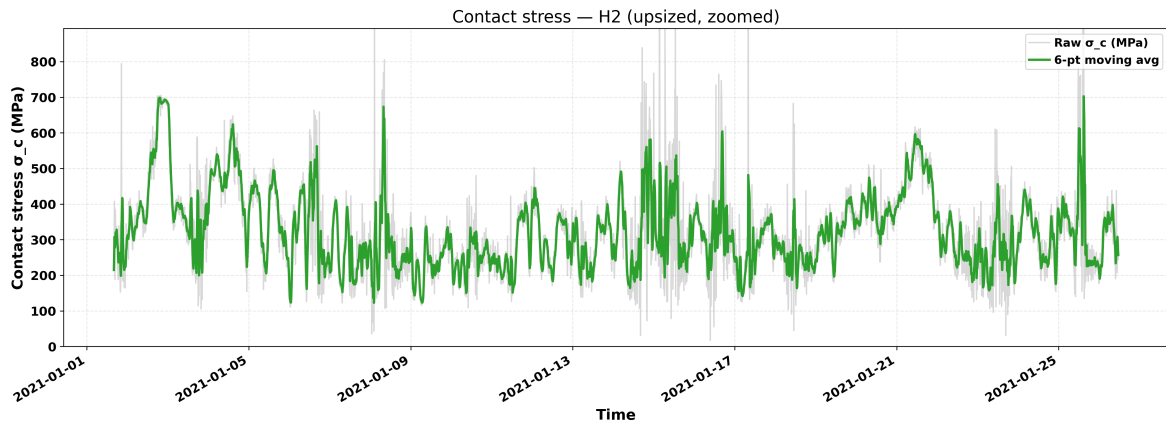


Figure 12: Contact stress  $\sigma_c$  time series for Helical Stage 2 (H2) pinion on the test set, showing raw values capped at the 99.5th percentile and the 6-point moving average.

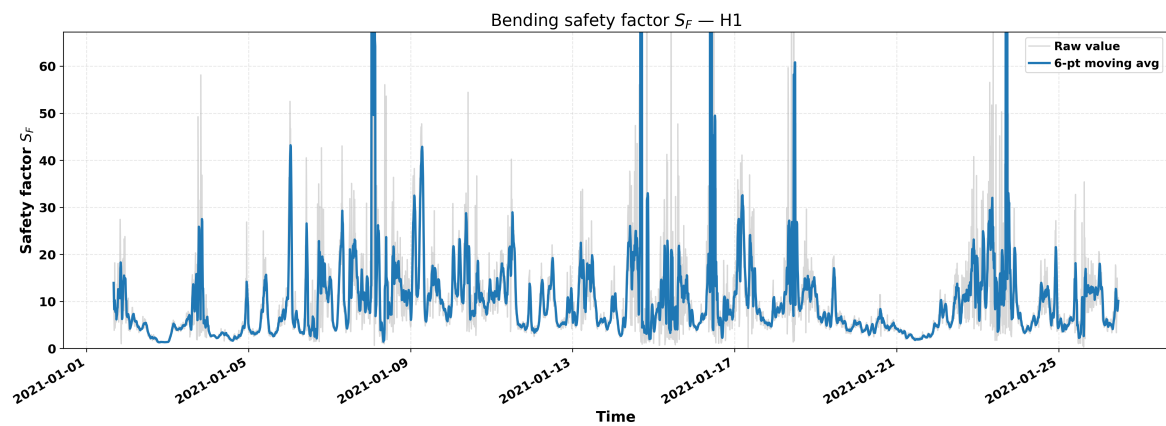


Figure 13: Bending safety factor  $S_F$  time series for Helical Stage 1 (H1) pinion on the test set, showing values capped at the 99.5th percentile and the 6-point moving average.

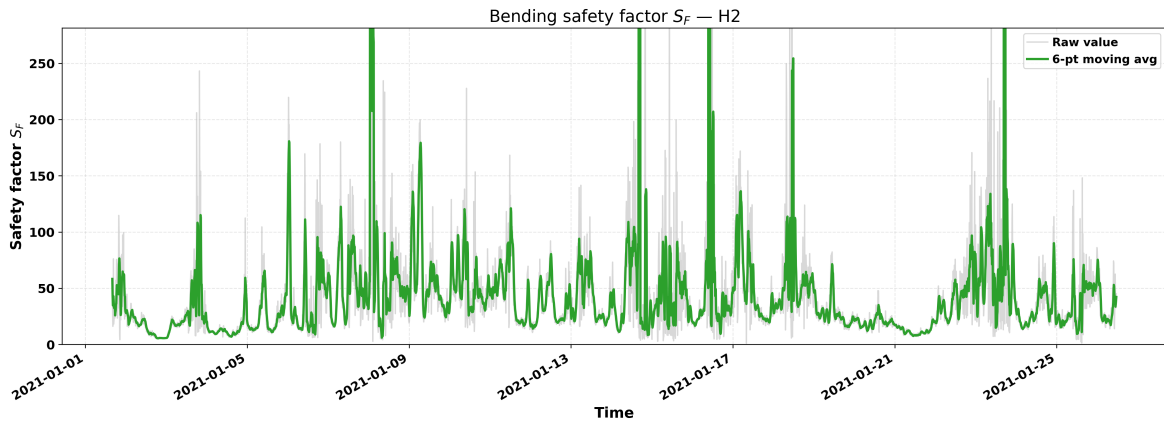


Figure 14: Bending safety factor  $S_F$  time series for Helical Stage 2 (H2) pinion on the test set, showing values capped at the 99.5th percentile and the 6-point moving average.

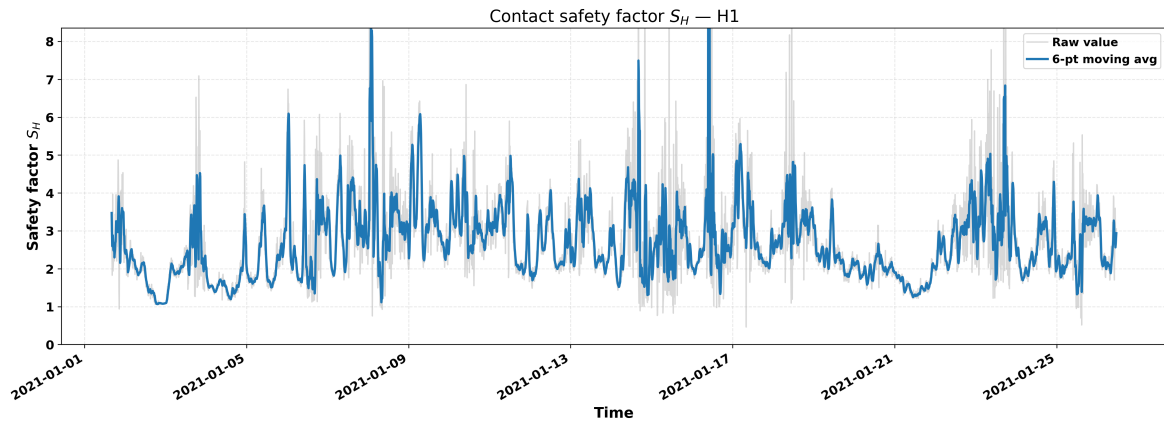


Figure 15: Contact safety factor  $S_H$  time series for Helical Stage 1 (H1) pinion on the test set, showing values capped at the 99.5th percentile and the 6-point moving average.

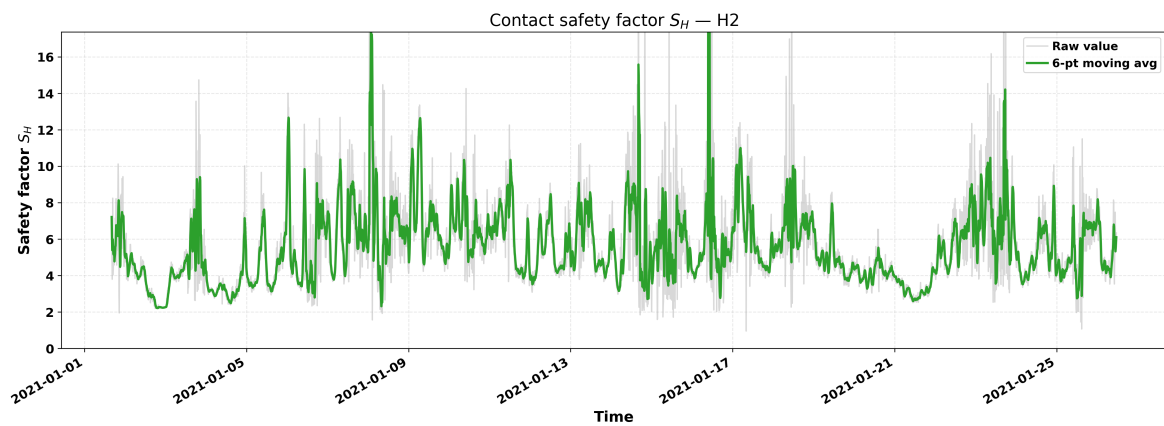


Figure 16: Contact safety factor  $S_H$  time series for Helical Stage 2 (H2) pinion on the test set, showing values capped at the 99.5th percentile and the 6-point moving average.

447 The similarity in patterns for  $W_t$ ,  $\sigma_b$ , and  $\sigma_c$  can be explained with the mesh load  $W_t$  is  
 448 responsible for driving both stress responses. The bending relation is approximately linear  
 449 in  $W_t$ ,

$$\sigma_b \propto W_t,$$

450 The contact relation is monotone through a square root,

$$\sigma_c \propto \sqrt{W_t}.$$

451 Therefore the timevarying shape of  $\sigma_b(t)$  and  $\sigma_c(t)$  follows  $W_t(t)$ . The square root compresses  
 452 peaks in  $\sigma_c$  relative to  $\sigma_b$ , but the temporal pattern remains aligned. Differences in level across  
 453 stages arise from stage-specific geometry and factors ( $d$ ,  $F$ ,  $J$ ,  $I$ ,  $K_v$ ,  $K_m$ ).

454 The (H1) and (H2)  $W_t$  series exhibit the expected stage ratio (H1 larger than H2 due  
 455 to drivetrain ratios and efficiencies). The moving average follows the operating envelope;  
 456 transient spikes are visible in the raw series. The 99.5<sup>th</sup> percentile cap is only a plotting aid  
 457 and is not used in any stress computation.

458 For H1, the 6-point average of  $\sigma_b$  lies mainly near the reference level for the pinion  
 459 with intermittent excursions during high-load intervals; H2 remains lower, consistent with its  
 460 larger  $J$ , larger pitch diameter, and lower stage load. The H1-to-H2 level difference agrees  
 461 with baseline geometry and factors, indicating correct implementation.

462 Contact stress magnitudes exceed bending (Hertz pressure) but remain mostly below the  
 463 99.5<sup>th</sup> percentile cap. H1 exceeds H2 because of higher  $W_t$ , smaller  $d$ , and slightly different  
 464  $K_v$ ,  $K_m$ ,  $I$ . Peaks are less sharp than in bending due to the square-root dependence.

- 465 1. Stage scaling is correct: H1 levels exceed H2 for  $W_t$ ,  $\sigma_b$ , and  $\sigma_c$ , matching train ratios  
 466 and geometry.
- 467 2. Shape coherence holds:  $W_t$ ,  $\sigma_b$ , and  $\sigma_c$  co-vary in time;  $\sigma_c$  is a compressed version of  
 468 the  $W_t$  pattern;  $\sigma_b$  is nearly proportional.
- 469 3. Factor influence behaves as expected: with time-invariant geometry and AGMA factors,  
 470 only levels shift between stages, not the temporal pattern.

471 Pinions are typically limiting because they have fewer teeth (lower  $J$ , higher  $\sigma_b$  for the  
 472 same  $W_t$ ), accumulate more load cycles for life factors, and, in the baseline, the mating gears  
 473 benefit from hardness ratio effects. Verifying pinions is conservative. The same pipeline can  
 474 be applied to gears by substituting the gear  $J$ , diameters, and life factors;  $\sigma_c(t)$  is the same  
 475 timeline but compared to gear allowables.

476 The figures provide stress histories consistent with the baseline geometry and factors. The  
 477 moving average highlights sustained levels; the percentile cap prevents rare spikes from domi-  
 478 nating axes. Absolute capacity and detailed life assessments require comparison with AGMA  
 479 allowables and life factors; the present plots quantify the stress demand only. Within this  
 480 scope, the results are internally consistent and technically plausible for the current baseline.

#### 481 4. Conclusion

482 This project presented an integrated framework that links SCADA based wind power  
 483 forecasting, drivetrain torque reconstruction, and AGMA gear stress analysis for a wind

484 turbine gearbox. A multivariate LSTM network was trained on 10-minute SCADA records,  
485 using wind speed, rotor speed, wind direction, yaw angle, and related operational signals to  
486 predict short-horizon electrical power output. The model achieved a test-set MAE of about  
487 79.5 kW ( $\approx 3.8\%$  of the 2.1 MW rated power), an RMSE of roughly 126.5 kW ( $\approx 6.0\%$ ), and  
488 a coefficient of determination  $R^2$ , indicating stable generalization across train, validation,  
489 and test splits for noisy field data. Directional error analysis showed that most wind sectors  
490 remain within 5–8% of rated power, with larger errors concentrated in a few inflow directions,  
491 that likely reflect wake or yaw effects rather than purely algorithmic limitations.

492 The predicted power time series was then converted to drivetrain torque using the mea-  
493 sured shaft speeds, and the resulting torque histories were compared against available SCADA  
494 torque measurements. After smoothing, the curves of actual and reconstructed torque almost  
495 overlap, with peak loads on the order of  $10^6$  Nm that are physically consistent with a 2.1 MW  
496 turbine operating at the observed rotor speeds. This confirms that the LSTM based power  
497 forecasts, combined with power to torque conversion, can reproduce both the magnitude and  
498 temporal pattern of the mechanical loading that drives gearbox degradation.

499 Building on this torque history, a three stage planetary–helical gearbox was sized following  
500 AGMA 2001-D04 guidance. The design employs a planetary input stage followed by two par-  
501 allel helical stages with practical tooth counts and carburized, hardened steel gears. Using the  
502 reconstructed torques, tangential tooth loads, bending stresses, and contact (pitting) stresses  
503 were computed for the helical pinions with all relevant AGMA modifying factors (overload,  
504 dynamics, size, load distribution, rim thickness, temperature, hardness ratio, and reliability).  
505 The time-varying bending and contact safety factors  $S_F(t)$  and  $S_H(t)$  remain greater than  
506 unity over all observed operating points, supporting the conclusion that the gearbox design  
507 is sufficient for the intended service life under the reconstructed torque spectrum.

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